

# The mFilter Package

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**Title** Miscellaneous time series filters

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**Depends** R (>= 2.2.0), stats

**Suggests** tseries, pastecs, locfit, tseriesChaos, RTisean, tsDyn, forecast

**Description** The package implements several time series filters useful for smoothing and extracting trend and cyclical components of a time series. The routines are commonly used in economics and finance, however they should also be interest to other areas. Currently, Christiano-Fitzgerald, Baxter-King, Hodrick-Prescott, Butterworth, and trigonometric regression filters are included in the package.

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**License** GPL version 2 or newer

**URL** <http://www.mbalcilar.net/mFilter>, <http://www.r-project.org>

## R topics documented:

bkfilter . . . . .	2
bwfilter . . . . .	4
cfilter . . . . .	7
hpfiler . . . . .	10
mFilter-methods . . . . .	13
mFilter-package . . . . .	14
mFilter . . . . .	18
trfilter . . . . .	21
unemp . . . . .	24
<b>Index</b>	<b>26</b>

bkfilter

*Baxter-King filter of a time series***Description**

This function implements the Baxter-King approximation to the band pass filter for a time series. The function computes cyclical and trend components of the time series using band-pass approximation for fixed and variable length filters.

**Usage**

```
bkfilter(x, pl=NULL, pu=NULL, nfix=NULL, type=c("fixed", "variable"), drift=FALSE)
```

**Arguments**

<code>x</code>	a regular time series
<code>type</code>	character, indicating the filter type, "fixed", for the fixed length Baxter-King filter (default), "variable", for the variable length Baxter-King filter.
<code>pl</code>	integer. minimum period of oscillation of desired component ( $pl \leq 2$ ).
<code>pu</code>	integer. maximum period of oscillation of desired component ( $2 \leq pl < pu < \infty$ ).
<code>drift</code>	logical, FALSE if no drift in time series (default), TRUE if drift in time series.
<code>nfix</code>	sets fixed lead/lag length or order of the filter. The <code>nfix</code> option sets the order of the filter by $2 * nfix + 1$ . The default is <code>frequency(x) * 3</code> .

**Details**

Almost all filters in this package can be put into the following framework. Given a time series  $\{x_t\}_{t=1}^T$  we are interested in isolating component of  $x_t$ , denoted  $y_t$  with period of oscillations between  $p_l$  and  $p_u$ , where  $2 \leq p_l < p_u < \infty$ .

Consider the following decomposition of the time series

$$x_t = y_t + \bar{x}_t$$

The component  $y_t$  is assumed to have power only in the frequencies in the interval  $\{(a, b) \cup (-a, -b)\} \in (-\pi, \pi)$ .  $a$  and  $b$  are related to  $p_l$  and  $p_u$  by

$$a = \frac{2\pi}{p_u} \quad b = \frac{2\pi}{p_l}$$

If infinite amount of data is available, then we can use the ideal bandpass filter

$$y_t = B(L)x_t$$

where the filter,  $B(L)$ , is given in terms of the lag operator  $L$  and defined as

$$B(L) = \sum_{j=-\infty}^{\infty} B_j L^j, \quad L^k x_t = x_{t-k}$$

The ideal bandpass filter weights are given by

$$B_j = \frac{\sin(jb) - \sin(ja)}{\pi j}$$

$$B_0 = \frac{b - a}{\pi}$$

The Baxter-King filter is a finite data approximation to the ideal bandpass filter with following moving average weights

$$y_t = \hat{B}(L)x_t = \sum_{j=-n}^n \hat{B}_j x_{t+j} = \hat{B}_0 x_t + \sum_{j=1}^n \hat{B}_j (x_{t-j} + x_{t+j})$$

where

$$\hat{B}_j = B_j - \frac{1}{2n+1} \sum_{j=-n}^n B_j$$

If `drift=TRUE` the drift adjusted series is obtained

$$\tilde{x}_t = x_t - t \left( \frac{x_T - x_1}{T - 1} \right), \quad t = 0, 1, \dots, T - 1$$

where  $\tilde{x}_t$  is the undrifted series.

### Value

A "mFilter" object (see [mFilter](#)).

### Author(s)

Mehmet Balcilar, (mbalcilar@yahoo.com)

### References

- M. Baxter and R.G. King. Measuring business cycles: Approximate bandpass filters. *The Review of Economics and Statistics*, 81(4):575-93, 1999.
- L. Christiano and T.J. Fitzgerald. The bandpass filter. *International Economic Review*, 44(2):435-65, 2003.
- J. D. Hamilton. *Time series analysis*. Princeton, 1994.
- R.J. Hodrick and E.C. Prescott. Postwar US business cycles: an empirical investigation. *Journal of Money, Credit, and Banking*, 29(1):1-16, 1997.
- R.G. King and S.T. Rebelo. Low frequency filtering and real business cycles. *Journal of Economic Dynamics and Control*, 17(1-2):207-31, 1993.
- D.S.G. Pollock. Trend estimation and de-trending via rational square-wave filters. *Journal of Econometrics*, 99:317-334, 2000.

### See Also

[mFilter](#), [bwfilter](#), [cfilter](#), [hpfilter](#), [trfilter](#)

**Examples**

```
## library(mFilter)

data(unemp)

opar <- par(no.readonly=TRUE)

unemp.bk <- bkfilter(unemp)
plot(unemp.bk)
unemp.bk1 <- bkfilter(unemp, drift=TRUE)
unemp.bk2 <- bkfilter(unemp, pl=8,pu=40,drift=TRUE)
unemp.bk3 <- bkfilter(unemp, pl=2,pu=60,drift=TRUE)
unemp.bk4 <- bkfilter(unemp, pl=2,pu=40,drift=TRUE)

par(mfrow=c(2,1),mar=c(3,3,2,1),cex=.8)
plot(unemp.bk1$x,
     main="Baxter-King filter of unemployment: Trend, drift=TRUE",
     col=1, ylab="")
lines(unemp.bk1$trend,col=2)
lines(unemp.bk2$trend,col=3)
lines(unemp.bk3$trend,col=4)
lines(unemp.bk4$trend,col=5)
legend("topleft",legend=c("series", "pl=2, pu=32", "pl=8, pu=40",
                          "pl=2, pu=60", "pl=2, pu=40"), col=1:5, lty=rep(1,5), ncol=1)

plot(unemp.bk1$cycle,
     main="Baxter-King filter of unemployment: Cycle,drift=TRUE",
     col=2, ylab="", ylim=range(unemp.bk3$cycle,na.rm=TRUE))
lines(unemp.bk2$cycle,col=3)
lines(unemp.bk3$cycle,col=4)
lines(unemp.bk4$cycle,col=5)
## legend("topleft",legend=c("pl=2, pu=32", "pl=8, pu=40", "pl=2, pu=60",
## "pl=2, pu=40"), col=1:5, lty=rep(1,5), ncol=1)

par(opar)
```

---

 bwfilter

*Butterworth filter of a time series*


---

**Description**

Filters a time series using the Butterworth square-wave highpass filter described in Pollock (2000).

**Usage**

```
bwfilter(x, freq=NULL, nfix=NULL, drift=FALSE)
```

**Arguments**

<code>x</code>	a regular time series
<code>nfix</code>	sets the order of the filter. The default is <code>nfix=2</code> , when <code>nfix=NULL</code> .
<code>freq</code>	integer, the cut-off frequency of the Butterworth filter. The default is <code>trunc(2.5*frequency(x))</code> .
<code>drift</code>	logical, FALSE if no drift in time series (default), TRUE if drift in time series.

**Details**

Almost all filters in this package can be put into the following framework. Given a time series  $\{x_t\}_{t=1}^T$  we are interested in isolating component of  $x_t$ , denoted  $y_t$  with period of oscillations between  $p_l$  and  $p_u$ , where  $2 \leq p_l < p_u < \infty$ .

Consider the following decomposition of the time series

$$x_t = y_t + \bar{x}_t$$

The component  $y_t$  is assumed to have power only in the frequencies in the interval  $\{(a, b) \cup (-a, -b)\} \in (-\pi, \pi)$ .  $a$  and  $b$  are related to  $p_l$  and  $p_u$  by

$$a = \frac{2\pi}{p_u} \quad b = \frac{2\pi}{p_l}$$

If infinite amount of data is available, then we can use the ideal bandpass filter

$$y_t = B(L)x_t$$

where the filter,  $B(L)$ , is given in terms of the lag operator  $L$  and defined as

$$B(L) = \sum_{j=-\infty}^{\infty} B_j L^j, \quad L^k x_t = x_{t-k}$$

The ideal bandpass filter weights are given by

$$B_j = \frac{\sin(jb) - \sin(ja)}{\pi j}$$

$$B_0 = \frac{b-a}{\pi}$$

The digital version of the Butterworth highpass filter is described by the rational polynomial expression (the filter's z-transform)

$$\frac{\lambda(1-z)^n(1-z^{-1})^n}{(1+z)^n(1+z^{-1})^n + \lambda(1-z)^n(1-z^{-1})^n}$$

The time domain version can be obtained by substituting  $z$  for the lag operator  $L$ .

Pollock derives a specialized finite-sample version of the Butterworth filter on the basis of signal extraction theory. Let  $s_t$  be the trend and  $c_t$  cyclical component of  $y_t$ , then these components are extracted as

$$y_t = s_t + c_t = \frac{(1+L)^n}{(1-L)^d} \nu_t + (1-L)^{n-d} \varepsilon_t$$

where  $\nu_t \sim N(0, \sigma_\nu^2)$  and  $\varepsilon_t \sim N(0, \sigma_\varepsilon^2)$ .

If `drift=TRUE` the drift adjusted series is obtained as

$$\tilde{x}_t = x_t - t \left( \frac{x_T - x_1}{T - 1} \right), \quad t = 0, 1, \dots, T - 1$$

where  $\tilde{x}_t$  is the undrifted series.

### Value

A "mFilter" object (see `mFilter`).

### Author(s)

Mehmet Balcilar, (mbalcilar@yahoo.com)

### References

M. Baxter and R.G. King. Measuring business cycles: Approximate bandpass filters. *The Review of Economics and Statistics*, 81(4):575-93, 1999.

L. Christiano and T.J. Fitzgerald. The bandpass filter. *International Economic Review*, 44(2):435-65, 2003.

J. D. Hamilton. *Time series analysis*. Princeton, 1994.

R.J. Hodrick and E.C. Prescott. Postwar US business cycles: an empirical investigation. *Journal of Money, Credit, and Banking*, 29(1):1-16, 1997.

R.G. King and S.T. Rebelo. Low frequency filtering and real business cycles. *Journal of Economic Dynamics and Control*, 17(1-2):207-31, 1993.

D.S.G. Pollock. Trend estimation and de-trending via rational square-wave filters. *Journal of Econometrics*, 99:317-334, 2000.

### See Also

`mFilter`, `hpfilter`, `cffilter`, `bkfilter`, `trfilter`

### Examples

```
## library(mFilter)

data(unemp)

opar <- par(no.readonly=TRUE)

unemp.bw <- bwfilter(unemp)
plot(unemp.bw)
unemp.bw1 <- bwfilter(unemp, drift=TRUE)
unemp.bw2 <- bwfilter(unemp, freq=8, drift=TRUE)
unemp.bw3 <- bwfilter(unemp, freq=10, nfix=3, drift=TRUE)
unemp.bw4 <- bwfilter(unemp, freq=10, nfix=4, drift=TRUE)
```

```

par(mfrow=c(2,1),mar=c(3,3,2,1),cex=.8)
plot(unemp.bw1$x,
     main="Butterworth filter of unemployment: Trend,
     drift=TRUE",col=1, ylab="")
lines(unemp.bw1$trend,col=2)
lines(unemp.bw2$trend,col=3)
lines(unemp.bw3$trend,col=4)
lines(unemp.bw4$trend,col=5)
legend("topleft",legend=c("series", "freq=10, nfix=2",
                          "freq=8, nfix=2", "freq=10, nfix=3", "freq=10, nfix=4"),
       col=1:5, lty=rep(1,5), ncol=1)

plot(unemp.bw1$cycle,
     main="Butterworth filter of unemployment: Cycle,drift=TRUE",
     col=2, ylab="", ylim=range(unemp.bw3$cycle,na.rm=TRUE))
lines(unemp.bw2$cycle,col=3)
lines(unemp.bw3$cycle,col=4)
lines(unemp.bw4$cycle,col=5)
## legend("topleft",legend=c("series", "freq=10, nfix=2", "freq=8,
## nfix=2", "freq## =10, nfix=3", "freq=10, nfix=4"), col=1:5,
## lty=rep(1,5), ncol=1)

par(opar)

```

---

cfilter

*Christiano-Fitzgerald filter of a time series*


---

## Description

This function implements the Christiano-Fitzgerald approximation to the ideal band pass filter for a time series. The function computes cyclical and trend components of the time series using several band-pass approximation strategies.

## Usage

```

cfilter(x,pl=NULL,pu=NULL,root=FALSE,drift=FALSE,
        type=c("asymmetric","symmetric","fixed","baxter-king","trigonometric"),
        nfix=NULL,theta=1)

```

## Arguments

x	a regular time series.
type	the filter type, "asymmetric", asymmetric Christiano-Fitzgerald filter (default), "symmetric", symmetric Christiano-Fitzgerald filter "fixed", fixed length Christiano-Fitzgerald filter, "baxter-king", Baxter-King fixed length symmetric filter, "trigonometric", trigonometric regression filter.
pl	minimum period of oscillation of desired component (pl<=2).
pu	maximum period of oscillation of desired component (2<=pl<pu<infinity).

root	logical, FALSE if no unit root in time series (default), TRUE if unit root in time series. The root option has no effect if type is "baxter-king" or "trigonometric".
drift	logical, FALSE if no drift in time series (default), TRUE if drift in time series.
nfix	sets fixed lead/lag length or order of the filter with "baxter-king" and "fixed". The nfix option sets the order of the filter by 2*nfix+1. The default is nfix=1.
theta	moving average coefficients for time series model: $x(t) = \mu + \text{root} * x(t-1) + \text{theta}(1) * e(t) + \text{theta}(2) * e(t-1) + \dots$ , where $e(t)$ is a white noise.

### Details

Almost all filters in this package can be put into the following framework. Given a time series  $\{x_t\}_{t=1}^T$  we are interested in isolating component of  $x_t$ , denoted  $y_t$  with period of oscillations between  $p_l$  and  $p_u$ , where  $2 \leq p_l < p_u < \infty$ .

Consider the following decomposition of the time series

$$x_t = y_t + \bar{x}_t$$

The component  $y_t$  is assumed to have power only in the frequencies in the interval  $\{(a, b) \cup (-a, -b)\} \in (-\pi, \pi)$ .  $a$  and  $b$  are related to  $p_l$  and  $p_u$  by

$$a = \frac{2\pi}{p_u} \quad b = \frac{2\pi}{p_l}$$

If infinite amount of data is available, then we can use the ideal bandpass filter

$$y_t = B(L)x_t$$

where the filter,  $B(L)$ , is given in terms of the lag operator  $L$  and defined as

$$B(L) = \sum_{j=-\infty}^{\infty} B_j L^j, \quad L^k x_t = x_{t-k}$$

The ideal bandpass filter weights are given by

$$B_j = \frac{\sin(jb) - \sin(ja)}{\pi j}$$

$$B_0 = \frac{b - a}{\pi}$$

The finite sample approximation to the ideal bandpass filter uses the alternative filter

$$y_t = \hat{B}(L)x_t = \sum_{j=-n_1}^{n_2} \hat{B}_{t,j} x_{t+j}$$

Here the weights,  $\hat{B}_{t,j}$ , of the approximation is a solution to

$$\hat{B}_{t,j} = \arg \min E\{(y_t - \hat{y}_t)^2\}$$



The Christiano-Fitzgerald filter is a finite data approximation to the ideal bandpass filter and minimizes the mean squared error defined in the above equation.

Several band-pass approximation strategies can be selected in the function `cfilter`. The default setting of `cfilter` returns the filtered data  $\hat{y}_t$  associated with the unrestricted optimal filter assuming no unit root, no drift and an iid filter.

If `theta` is not equal to 1 the series is assumed to follow a moving average process. The moving average weights are given by `theta`. The default is `theta=1` (iid series). If `theta=`  $(\theta_1, \theta_2, \dots)$  then the series is assumed to be

$$x_t = \mu + 1_{root}x_{t-1} + \theta_1e_t + \theta_2e_{t-1} + \dots$$

where  $1_{root} = 1$  if the option `root=1` and  $1_{root} = 0$  if the option `root=0`, and  $e_t$  is a white noise.

If `drift=TRUE` the drift adjusted series is obtained as

$$\tilde{x}_t = x_t - t \left( \frac{x_T - x_1}{T - 1} \right), \quad t = 0, 1, \dots, T - 1$$

where  $\tilde{x}_t$  is the undrifted series.

### Value

A "mFilter" object (see `mFilter`).

### Author(s)

Mehmet Balcilar, (mbalcilar@yahoo.com)

### References

- M. Baxter and R.G. King. Measuring business cycles: Approximate bandpass filters. *The Review of Economics and Statistics*, 81(4):575-93, 1999.
- L. Christiano and T.J. Fitzgerald. The bandpass filter. *International Economic Review*, 44(2):435-65, 2003.
- J. D. Hamilton. *Time series analysis*. Princeton, 1994.
- R.J. Hodrick and E.C. Prescott. Postwar US business cycles: an empirical investigation. *Journal of Money, Credit, and Banking*, 29(1):1-16, 1997.
- R.G. King and S.T. Rebelo. Low frequency filtering and real business cycles. *Journal of Economic Dynamics and Control*, 17(1-2):207-31, 1993.
- D.S.G. Pollock. Trend estimation and de-trending via rational square-wave filters. *Journal of Econometrics*, 99:317-334, 2000.

### See Also

`mFilter`, `bwfilter`, `bkfilter`, `hpfiler`, `trfilter`

**Examples**

```
## library(mFilter)

data(unemp)

opar <- par(no.readonly=TRUE)

unemp.cf <- cffilter(unemp)
plot(unemp.cf)
unemp.cf1 <- cffilter(unemp, drift=TRUE, root=TRUE)
unemp.cf2 <- cffilter(unemp, pl=8,pu=40,drift=TRUE, root=TRUE)
unemp.cf3 <- cffilter(unemp, pl=2,pu=60,drift=TRUE, root=TRUE)
unemp.cf4 <- cffilter(unemp, pl=2,pu=40,drift=TRUE, root=TRUE,theta=c(.1,.4))

par(mfrow=c(2,1),mar=c(3,3,2,1),cex=.8)
plot(unemp.cf1$x,
main="Christiano-Fitzgerald filter of unemployment: Trend \n root=TRUE,drift=TRUE",
col=1, ylab="")
lines(unemp.cf1$trend,col=2)
lines(unemp.cf2$trend,col=3)
lines(unemp.cf3$trend,col=4)
lines(unemp.cf4$trend,col=5)
legend("topleft",legend=c("series", "pl=2, pu=32", "pl=8, pu=40", "pl=2, pu=60",
"pl=2, pu=40, theta=.1,.4"), col=1:5, lty=rep(1,5), ncol=1)

plot(unemp.cf1$cycle,
main="Christiano-Fitzgerald filter of unemployment: Cycle \n root=TRUE,drift=TRUE",
col=2, ylab="", ylim=range(unemp.cf3$cycle))
lines(unemp.cf2$cycle,col=3)
lines(unemp.cf3$cycle,col=4)
lines(unemp.cf4$cycle,col=5)
## legend("topleft",legend=c("pl=2, pu=32", "pl=8, pu=40", "pl=2, pu=60",
## "pl=2, pu=40, theta=.1,.4"), col=2:5, lty=rep(1,4), ncol=2)

par(opar)
```

---

hpfilter

*Hodrick-Prescott filter of a time series*


---

**Description**

This function implements the Hodrick-Prescott for estimating cyclical and trend component of a time series. The function computes cyclical and trend components of the time series using a frequency cut-off or smoothness parameter.

**Usage**

```
hpfilter(x, freq=NULL, type=c("lambda", "frequency"), drift=FALSE)
```

**Arguments**

x	a regular time series.
type	character, indicating the filter type, "lambda", for the filter that uses smoothness penalty parameter of the Hodrick-Prescott filter (default), "frequency", for the filter that uses a frequency cut-off type Hodrick-Prescott filter. These are related by $\lambda = (2 * \sin(\pi / \text{frequency}))^{-4}$ .
freq	integer, if type="lambda" then freq is the smoothing parameter (lambda) of the Hodrick-Prescott filter, if type="frequency" then freq is the cut-off frequency of the Hodrick-Prescott filter.
drift	logical, FALSE if no drift in time series (default), TRUE if drift in time series.

**Details**

Almost all filters in this package can be put into the following framework. Given a time series  $\{x_t\}_{t=1}^T$  we are interested in isolating component of  $x_t$ , denoted  $y_t$  with period of oscillations between  $p_l$  and  $p_u$ , where  $2 \leq p_l < p_u < \infty$ .

Consider the following decomposition of the time series

$$x_t = y_t + \bar{x}_t$$

The component  $y_t$  is assumed to have power only in the frequencies in the interval  $\{(a, b) \cup (-a, -b)\} \in (-\pi, \pi)$ .  $a$  and  $b$  are related to  $p_l$  and  $p_u$  by

$$a = \frac{2\pi}{p_u} \quad b = \frac{2\pi}{p_l}$$

If infinite amount of data is available, then we can use the ideal bandpass filter

$$y_t = B(L)x_t$$

where the filter,  $B(L)$ , is given in terms of the lag operator  $L$  and defined as

$$B(L) = \sum_{j=-\infty}^{\infty} B_j L^j, \quad L^k x_t = x_{t-k}$$

The ideal bandpass filter weights are given by

$$B_j = \frac{\sin(jb) - \sin(ja)}{\pi j}$$

$$B_0 = \frac{b - a}{\pi}$$

The Hodrick-Prescott filter obtains the filter weights  $\hat{B}_j$  as a solution to

$$\hat{B}_j = \arg \min E\{(y_t - \hat{y}_t)^2\} = \arg \min \left\{ \sum_{t=1}^T (y_t - \hat{y}_t)^2 + \lambda \sum_{t=2}^{T-1} (\hat{y}_{t+1} - 2\hat{y}_t + \hat{y}_{t-1})^2 \right\}$$

The Hodrick-Prescott filter is a finite data approximation with following moving average weights

$$\hat{B}_j = \frac{1}{2\pi} \int_{-\pi}^{\pi} \frac{4\lambda(1 - \cos(\omega))^2}{1 + 4\lambda(1 - \cos(\omega))^2} e^{i\omega j} d\omega$$

If `drift=TRUE` the drift adjusted series is obtained as

$$\tilde{x}_t = x_t - t \left( \frac{x_T - x_1}{T - 1} \right), \quad t = 0, 1, \dots, T - 1$$

where  $\tilde{x}_t$  is the undrifted series.

### Value

A "mFilter" object (see `mFilter`).

### Author(s)

Mehmet Balcilar, (`mbalcilar@yahoo.com`)

### References

- M. Baxter and R.G. King. Measuring business cycles: Approximate bandpass filters. *The Review of Economics and Statistics*, 81(4):575-93, 1999.
- L. Christiano and T.J. Fitzgerald. The bandpass filter. *International Economic Review*, 44(2):435-65, 2003.
- J. D. Hamilton. *Time series analysis*. Princeton, 1994.
- R.J. Hodrick and E.C. Prescott. Postwar US business cycles: an empirical investigation. *Journal of Money, Credit, and Banking*, 29(1):1-16, 1997.
- R.G. King and S.T. Rebelo. Low frequency filtering and real business cycles. *Journal of Economic Dynamics and Control*, 17(1-2):207-31, 1993.
- D.S.G. Pollock. Trend estimation and de-trending via rational square-wave filters. *Journal of Econometrics*, 99:317-334, 2000.

### See Also

`mFilter`, `bwfilter`, `cffilter`, `bkfilter`, `trfilter`

### Examples

```
## library(mFilter)

data(unemp)

opar <- par(no.readonly=TRUE)

unemp.hp <- hpfilter(unemp)
plot(unemp.hp)
unemp.hp1 <- hpfilter(unemp, drift=TRUE)
```

```

unemp.hp2 <- hpfilter(unemp, freq=800, drift=TRUE)
unemp.hp3 <- hpfilter(unemp, freq=12,type="frequency",drift=TRUE)
unemp.hp4 <- hpfilter(unemp, freq=52,type="frequency",drift=TRUE)

par(mfrow=c(2,1),mar=c(3,3,2,1),cex=.8)
plot(unemp.hp1$x, ylim=c(2,13),
main="Hodrick-Prescott filter of unemployment: Trend, drift=TRUE",
col=1, ylab="")
lines(unemp.hp1$trend,col=2)
lines(unemp.hp2$trend,col=3)
lines(unemp.hp3$trend,col=4)
lines(unemp.hp4$trend,col=5)
legend("topleft",legend=c("series", "lambda=1600", "lambda=800",
"freq=12", "freq=52"), col=1:5, lty=rep(1,5), ncol=1)

plot(unemp.hp1$cycle,
main="Hodrick-Prescott filter of unemployment: Cycle,drift=TRUE",
col=2, ylab="", ylim=range(unemp.hp4$cycle,na.rm=TRUE))
lines(unemp.hp2$cycle,col=3)
lines(unemp.hp3$cycle,col=4)
lines(unemp.hp4$cycle,col=5)
## legend("topleft",legend=c("lambda=1600", "lambda=800",
## "freq=12", "freq=52"), col=1:5, lty=rep(1,5), ncol=1)

par(opar)

```

---

mFilter-methods      *Methods for mFilter objects*

---

## Description

Common methods for all `mFilter` objects usually created by the `mFilter` function.

## Usage

```

## S3 method for class 'mFilter':
residuals(object, ...)
## S3 method for class 'mFilter':
fitted(object, ...)
## S3 method for class 'mFilter':
print(x, digits = max(3, getOption("digits") - 3), ...)
## S3 method for class 'mFilter':
plot(x, reference.grid = TRUE, col = "steelblue", ask=interactive(), ...)
## S3 method for class 'mFilter':
summary(object, digits = max(3, getOption("digits") - 3), ...)

```

## Arguments

`object, x`      an object of class "mFilter"; usually, a result of a call to `mFilter`.

digits	number of digits used for printing (see <a href="#">print</a> ).
col	color of the graph (see <a href="#">plot</a> ).
ask	logical. if TRUE the user is asked for input before a new graph drawn in an interactive session (see <a href="#">interactive</a> ).
reference.grid	logical. if true grid lines are drawn.
...	further arguments passed to or from other methods.

**Value**

for residuals and fitted a univariate time series; for plot, print, and summary the "mFilter" object.

**Author(s)**

Mehmet Balcilar, (mbalcilar@yahoo.com)

**See Also**

[mFilter](#) for the function that returns an objects of class "mFilter". Other functions which return objects of class "mFilter" are [bkfilter](#), [bwfilter](#), [cfilter](#), [bkfilter](#), [trfilter](#).

**Examples**

```
## library(mFilter)

data(unemp)

opar <- par(no.readonly=TRUE)

unemp.hp <- mFilter(unemp, filter="HP") # Hodrick-Prescott filter
print(unemp.hp)
summary(unemp.hp)
residuals(unemp.hp)
fitted(unemp.hp)
plot(unemp.hp)

par(opar)
```

**Description**

Getting started with the mFilter package

## Details

This package provides some tools for decomposing time series into trend (smooth) and cyclical (irregular) components. The package implements some commonly used filters such as the Hodrick-Prescott, Baxter-King and Christiano-Fitzgerald filter.

For loading the package, type:

```
library(mFilter)
```

A good place to start learning the package usage is to examine examples for the `mFilter` function. At the R prompt, write:

```
example("mFilter")
```

For a full list of functions exported by the package, type:

```
ls("package:mFilter")
```

Each exported function has a corresponding man page (some man pages are common to more functions). Display it by typing

```
help(functionName).
```

Almost all filters in this package can be put into the following framework. Given a time series  $\{x_t\}_{t=1}^T$  we are interested in isolating component of  $x_t$ , denoted  $y_t$  with period of oscillations between  $p_l$  and  $p_u$ , where  $2 \leq p_l < p_u < \infty$ .

Consider the following decomposition of the time series

$$x_t = y_t + \bar{x}_t$$

The component  $y_t$  is assumed to have power only in the frequencies in the interval  $\{(a, b) \cup (-a, -b)\} \in (-\pi, \pi)$ .  $a$  and  $b$  are related to  $p_l$  and  $p_u$  by

$$a = \frac{2\pi}{p_u} \quad b = \frac{2\pi}{p_l}$$

If infinite amount of data is available, then we can use the ideal bandpass filter

$$y_t = B(L)x_t$$

where the filter,  $B(L)$ , is given in terms of the lag operator  $L$  and defined as

$$B(L) = \sum_{j=-\infty}^{\infty} B_j L^j, \quad L^k x_t = x_{t-k}$$

The ideal bandpass filter weights are given by

$$B_j = \frac{\sin(jb) - \sin(ja)}{\pi j}$$

$$B_0 = \frac{b - a}{\pi}$$

The finite sample approximation to the ideal bandpass filter uses the alternative filter

$$y_t = \hat{B}(L)x_t = \sum_{j=-n_1}^{n_2} \hat{B}_{t,j} x_{t+j}$$

Here the weights,  $\hat{B}_{t,j}$ , of the approximation is a solution to

$$\hat{B}_{t,j} = \arg \min E\{(y_t - \hat{y}_t)^2\}$$

The Christiano-Fitzgerald filter is a finite data approximation to the ideal bandpass filter and minimizes the mean squared error defined in the above equation.

Several band-pass approximation strategies can be selected in the function `cffilter`. The default setting of `cffilter` returns the filtered data  $\hat{y}_t$  associated with the unrestricted optimal filter assuming no unit root, no drift and an iid filter.

If `theta` is not equal to 1 the series is assumed to follow a moving average process. The moving average weights are given by `theta`. The default is `theta=1` (iid series). If `theta=`  $(\theta_1, \theta_2, \dots)$  then the series is assumed to be

$$x_t = \mu + 1_{root}x_{t-1} + \theta_1e_t + \theta_2e_{t-1} + \dots$$

where  $1_{root} = 1$  if the option `root=1` and  $1_{root} = 0$  if the option `root=0`, and  $e_t$  is a white noise.

The Baxter-King filter is a finite data approximation to the ideal bandpass filter with following moving average weights

$$y_t = \hat{B}(L)x_t = \sum_{j=-n}^n \hat{B}_j x_{t+j} = \hat{B}_0 x_t + \sum_{j=1}^n \hat{B}_j (x_{t-j} + x_{t+j})$$

where

$$\hat{B}_j = B_j - \frac{1}{2n+1} \sum_{j=-n}^n B_j$$

The Hodrick-Prescott filter obtains the filter weights  $\hat{B}_j$  as a solution to

$$\hat{B}_j = \arg \min E\{(y_t - \hat{y}_t)^2\} = \arg \min \left\{ \sum_{t=1}^T (y_t - \hat{y}_t)^2 + \lambda \sum_{t=2}^{T-1} (\hat{y}_{t+1} - 2\hat{y}_t + \hat{y}_{t-1})^2 \right\}$$

The Hodrick-Prescott filter is a finite data approximation with following moving average weights

$$\hat{B}_j = \frac{1}{2\pi} \int_{-\pi}^{\pi} \frac{4\lambda(1 - \cos(\omega))^2}{1 + 4\lambda(1 - \cos(\omega))^2} e^{i\omega j} d\omega$$

The digital version of the Butterworth highpass filter is described by the rational polynomial expression (the filter's z-transform)

$$\frac{\lambda(1-z)^n(1-z^{-1})^n}{(1+z)^n(1+z^{-1})^n + \lambda(1-z)^n(1-z^{-1})^n}$$

The time domain version can be obtained by substituting  $z$  for the lag operator  $L$ .

Pollock (2000) derives a specialized finite-sample version of the Butterworth filter on the basis of signal extraction theory. Let  $s_t$  be the trend and  $c_t$  cyclical component of  $y_t$ , then these components are extracted as

$$y_t = s_t + c_t = \frac{(1+L)^n}{(1-L)^d} \nu_t + (1-L)^{n-d} \varepsilon_t$$



where  $\nu_t \sim N(0, \sigma_\nu^2)$  and  $\varepsilon_t \sim N(0, \sigma_\varepsilon^2)$ .

Let  $T$  be even and define  $n_1 = T/p_u$  and  $n_2 = T/p_l$ . The trigonometric regression filter is based on the following relation

$$y_t = \sum_{j=n_2}^{n_1} \{a_j \cos(\omega_j t) + b_j \sin(\omega_j t)\}$$

where  $a_j$  and  $b_j$  are the coefficients obtained by regressing  $x_t$  on the indicated sine and cosine functions. Specifically,

$$a_j = \frac{T}{2} \sum_{t=1}^T \cos(\omega_j t) x_t, \quad \text{for } j = 1, \dots, T/2 - 1$$

$$a_j = \frac{T}{2} \sum_{t=1}^T \cos(\pi t) x_t, \quad \text{for } j = T/2$$

and

$$b_j = \frac{T}{2} \sum_{t=1}^T \sin(\omega_j t) x_t, \quad \text{for } j = 1, \dots, T/2 - 1$$

$$b_j = \frac{T}{2} \sum_{t=1}^T \sin(\pi t) x_t, \quad \text{for } j = T/2$$

Let  $\hat{B}(L)x_t$  be the trigonometric regression filter. It can be showed that  $\hat{B}(1) = 0$ , so that  $\hat{B}(L)$  has a unit root for  $t = 1, 2, \dots, T$ . Also, when  $\hat{B}(L)$  is symmetric, it has a second unit root in the middle of the data for  $t$ . Therefore it is important to drift adjust data before it is filtered with a trigonometric regression filter.

If `drift=TRUE` the drift adjusted series is obtained as

$$\tilde{x}_t = x_t - t \left( \frac{x_T - x_1}{T - 1} \right), \quad t = 0, 1, \dots, T - 1$$

where  $\tilde{x}_t$  is the undrifted series.

### Author(s)

Mehmet Balcilar, (mbalcilar@yahoo.com)

### References

- M. Baxter and R.G. King. Measuring business cycles: Approximate bandpass filters. *The Review of Economics and Statistics*, 81(4):575-93, 1999.
- L. Christiano and T.J. Fitzgerald. The bandpass filter. *International Economic Review*, 44(2):435-65, 2003.
- J. D. Hamilton. *Time series analysis*. Princeton, 1994.
- R.J. Hodrick and E.C. Prescott. Postwar US business cycles: an empirical investigation. *Journal of Money, Credit, and Banking*, 29(1):1-16, 1997.
- R.G. King and S.T. Rebelo. Low frequency filtering and real business cycles. *Journal of Economic Dynamics and Control*, 17(1-2):207-31, 1993.
- D.S.G. Pollock. Trend estimation and de-trending via rational square-wave filters. *Journal of Econometrics*, 99:317-334, 2000.

**See Also**

[mFilter-methods](#) for listing all currently available `mFilter` methods. For help on common interface function `"mFilter"`, `mFilter`. For individual filter function usage, `bwfilter`, `bkfilter`, `cffilter`, `hpfiler`, `trfilter`.

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<code>mFilter</code>	<i>Decomposition of a time series into trend and cyclical components using various filters</i>
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---

**Description**

`mFilter` is a generic function for filtering time series data. The function invokes particular *filters* which depend on filter type specified via its argument `filter`. The filters implemented in the package `mFilter` package are useful for smoothing, and estimating trend and cyclical components. Some of these filters are commonly used in economics and finance for estimating cyclical component of time series.

The `mFilter` currently applies only to time series objects. However a default method is available and should work for any `numeric` or `vector` object.

**Usage**

```
mFilter(x, ...)
## Default S3 method:
mFilter(x, ...)
## S3 method for class 'ts':
mFilter(x, filter=c("HP", "BK", "CF", "BW", "TR"), ...)
```

**Arguments**

<code>x</code>	a regular a time series.
<code>filter</code>	filter type, the filter types are "HP" (Hodrick-Prescott), "BK" (Baxter-King), "CF" (Christiano-Fitzgerald), "BW" (Butterworth), and "TR" (trigonometric regression).
<code>...</code>	Additional arguments to pass to the relevant filter functions. These are passed to <code>hpfiler</code> , <code>bkfilter</code> , <code>cffilter</code> , <code>bwfilter</code> , and <code>trfilter</code> , respectively for the "HP", "BK", "CF", "BW", and "TR" filters.

**Details**

The default behaviour is to apply the default filter to `ts` objects.

**Value**

An object of class "mFilter".

The function `summary` is used to obtain and print a summary of the results, while the function `plot` produces a plot of the original series, the trend, and the cyclical components. The function `print` is also available for displaying estimation results.

The generic accessor functions `fitted` and `residuals` extract estimated trend and cyclical components of an "mFilter" object, respectively.

An object of class "mFilter" is a list containing at least the following elements:

<code>cycle</code>	Estimated cyclical (irregular) component of the series.
<code>trend</code>	Estimated trend (smooth) component of the series.
<code>fmatrix</code>	The filter matrix applied to original series.
<code>method</code>	The method, if available, for the filter type applied.
<code>type</code>	The filter type applied to the series.
<code>call</code>	Call to the function.
<code>title</code>	The title for displaying results.
<code>xname</code>	Name of the series passed to <code>mFilter</code> for filtering.
<code>x</code>	The original or drift adjusted, if <code>drift=TRUE</code> , time series passed to the <code>mFilter</code> .
<code>nfix</code>	Length or order of the fixed length filters.
<code>pl</code>	Minimum period of oscillation of desired component ( $2 \leq pl$ ).
<code>pu</code>	Maximum period of oscillation of desired component ( $2 \leq pl < pu < \infty$ ).
<code>lambda</code>	Lambda (smoothness) parameter of the HP filter.
<code>root</code>	Whether time series has a unit root, TRUE or FALSE (default).
<code>drift</code>	Whether time series has drift, TRUE or FALSE (default).
<code>theta</code>	MA coefficients for time series model, used in "CF" filter.

**Author(s)**

Mehmet Balcilar, (mbalcilar@yahoo.com)

**See Also**

Other functions which return objects of class "mFilter" are `bkfilter`, `bwfilter`, `cffilter`, `bkfilter`, `trfilter`. Following functions apply the relevant methods to an object of the "mFilter" class: `print.mFilter`, `summary.mFilter`, `plot.mFilter`, `fitted.mFilter`, `residuals.mFilter`.

**Examples**

```
## library(mFilter)

data(unemp)

opar <- par(no.readonly=TRUE)
```

```

unemp.hp <- mFilter(unemp,filter="HP") # Hodrick-Prescott filter
print(unemp.hp)
summary(unemp.hp)
residuals(unemp.hp)
fitted(unemp.hp)
plot(unemp.hp)

unemp.bk <- mFilter(unemp,filter="BK") # Baxter-King filter
unemp.cf <- mFilter(unemp,filter="CF") # Christiano-Fitzgerald filter
unemp.bw <- mFilter(unemp,filter="BW") # Butterworth filter
unemp.tr <- mFilter(unemp,filter="TR") # Trigonometric regression filter

par(mfrow=c(2,1),mar=c(3,3,2,1),cex=.8)
plot(unemp,main="Unemployment Series & Estimated Trend", col=1, ylab="")
lines(unemp.hp$trend,col=2)
lines(unemp.bk$trend,col=3)
lines(unemp.cf$trend,col=4)
lines(unemp.bw$trend,col=5)
lines(unemp.tr$trend,col=6)

legend("topleft",legend=c("series", "HP", "BK", "CF", "BW", "TR"),
      col=1:6,lty=rep(1,6),ncol=2)

plot(unemp.hp$cycle,main="Estimated Cyclical Component",
      ylim=c(-2,2.5),col=2,ylab="")
lines(unemp.bk$cycle,col=3)
lines(unemp.cf$cycle,col=4)
lines(unemp.bw$cycle,col=5)
lines(unemp.tr$cycle,col=6)
## legend("topleft",legend=c("HP", "BK", "CF", "BW", "TR"),
## col=2:6,lty=rep(1,5),ncol=2)

unemp.cf1 <- mFilter(unemp,filter="CF", drift=TRUE, root=TRUE)
unemp.cf2 <- mFilter(unemp,filter="CF", pl=8,pu=40,drift=TRUE, root=TRUE)
unemp.cf3 <- mFilter(unemp,filter="CF", pl=2,pu=60,drift=TRUE, root=TRUE)
unemp.cf4 <- mFilter(unemp,filter="CF", pl=2,pu=40,drift=TRUE,
                    root=TRUE,theta=c(.1,.4))

plot(unemp,
     main="Christiano-Fitzgerald filter of unemployment: Trend \n root=TRUE,drift=TRUE",
     col=1, ylab="")
lines(unemp.cf1$trend,col=2)
lines(unemp.cf2$trend,col=3)
lines(unemp.cf3$trend,col=4)
lines(unemp.cf4$trend,col=5)
legend("topleft",legend=c("series", "pl=2, pu=32", "pl=8, pu=40",
                        "pl=2, pu=60", "pl=2, pu=40, theta=.1,.4"), col=1:5, lty=rep(1,5), ncol=1)

plot(unemp.cf1$cycle,
     main="Christiano-Fitzgerald filter of unemployment: Cycle \n root=TRUE,drift=TRUE",
     col=2, ylab="", ylim=range(unemp.cf3$cycle))
lines(unemp.cf2$cycle,col=3)

```

```

lines(unemp.cf3$cycle,col=4)
lines(unemp.cf4$cycle,col=5)
## legend("topleft",legend=c("pl=2, pu=32", "pl=8, pu=40", "pl=2, pu=60",
## "pl=2, pu=40, theta=.1,.4"), col=2:5, lty=rep(1,4), ncol=2)

par(opar)

```

trfilter

*Trigonometric regression filter of a time series***Description**

This function uses trigonometric regression filter for estimating cyclical and trend components of a time series. The function computes cyclical and trend components of the time series using a lower and upper cut-off frequency in the spirit of a band pass filter.

**Usage**

```
trfilter(x,pl=NULL,pu=NULL,drift=FALSE)
```

**Arguments**

x	a regular time series.
pl	integer. minimum period of oscillation of desired component ( $pl \leq 2$ ).
pu	integer. maximum period of oscillation of desired component ( $2 \leq pl < pu < \infty$ ).
drift	logical, FALSE if no drift in time series (default), TRUE if drift in time series.

**Details**

Almost all filters in this package can be put into the following framework. Given a time series  $\{x_t\}_{t=1}^T$  we are interested in isolating component of  $x_t$ , denoted  $y_t$  with period of oscillations between  $p_l$  and  $p_u$ , where  $2 \leq p_l < p_u < \infty$ .

Consider the following decomposition of the time series

$$x_t = y_t + \bar{x}_t$$

The component  $y_t$  is assumed to have power only in the frequencies in the interval  $\{(a, b) \cup (-a, -b)\} \in (-\pi, \pi)$ .  $a$  and  $b$  are related to  $p_l$  and  $p_u$  by

$$a = \frac{2\pi}{p_u} \quad b = \frac{2\pi}{p_l}$$

If infinite amount of data is available, then we can use the ideal bandpass filter

$$y_t = B(L)x_t$$

where the filter,  $B(L)$ , is given in terms of the lag operator  $L$  and defined as

$$B(L) = \sum_{j=-\infty}^{\infty} B_j L^j, \quad L^k x_t = x_{t-k}$$

The ideal bandpass filter weights are given by

$$B_j = \frac{\sin(jb) - \sin(ja)}{\pi j}$$

$$B_0 = \frac{b-a}{\pi}$$

Let  $T$  be even and define  $n_1 = T/p_u$  and  $n_2 = T/p_l$ . The trigonometric regression filter is based on the following relation

$$y_t = \sum_{j=n_2}^{n_1} \{a_j \cos(\omega_j t) + b_j \sin(\omega_j t)\}$$

where  $a_j$  and  $b_j$  are the coefficients obtained by regressing  $x_t$  on the indicated sine and cosine functions. Specifically,

$$a_j = \frac{T}{2} \sum_{t=1}^T \cos(\omega_j t) x_t, \quad \text{for } j = 1, \dots, T/2 - 1$$

$$a_j = \frac{T}{2} \sum_{t=1}^T \cos(\pi t) x_t, \quad \text{for } j = T/2$$

and

$$b_j = \frac{T}{2} \sum_{t=1}^T \sin(\omega_j t) x_t, \quad \text{for } j = 1, \dots, T/2 - 1$$

$$b_j = \frac{T}{2} \sum_{t=1}^T \sin(\pi t) x_t, \quad \text{for } j = T/2$$

Let  $\hat{B}(L)x_t$  be the trigonometric regression filter. It can be showed that  $\hat{B}(1) = 0$ , so that  $\hat{B}(L)$  has a unit root for  $t = 1, 2, \dots, T$ . Also, when  $\hat{B}(L)$  is symmetric, it has a second unit root in the middle of the data for  $t$ . Therefore it is important to drift adjust data before it is filtered with a trigonometric regression filter.

If `drift=TRUE` the drift adjusted series is obtained as

$$\tilde{x}_t = x_t - t \left( \frac{x_T - x_1}{T - 1} \right), \quad t = 0, 1, \dots, T - 1$$

where  $\tilde{x}_t$  is the undrifted series.

### Value

A "mFilter" object (see [mFilter](#)).

### Author(s)

Mehmet Balcilar, (mbalcilar@yahoo.com)

## References

- M. Baxter and R.G. King. Measuring business cycles: Approximate bandpass filters. *The Review of Economics and Statistics*, 81(4):575-93, 1999.
- L. Christiano and T.J. Fitzgerald. The bandpass filter. *International Economic Review*, 44(2):435-65, 2003.
- J. D. Hamilton. *Time series analysis*. Princeton, 1994.
- R.J. Hodrick and E.C. Prescott. Postwar US business cycles: an empirical investigation. *Journal of Money, Credit, and Banking*, 29(1):1-16, 1997.
- R.G. King and S.T. Rebelo. Low frequency filtering and real business cycles. *Journal of Economic Dynamics and Control*, 17(1-2):207-31, 1993.
- D.S.G. Pollock. Trend estimation and de-trending via rational square-wave filters. *Journal of Econometrics*, 99:317-334, 2000.

## See Also

[mFilter](#), [hpfilter](#), [cfilter](#), [bkfilter](#), [bwfilter](#)

## Examples

```
## library(mFilter)

data(unemp)

opar <- par(no.readonly=TRUE)

unemp.tr <- trfilter(unemp, drift=TRUE)
plot(unemp.tr)
unemp.tr1 <- trfilter(unemp, drift=TRUE)
unemp.tr2 <- trfilter(unemp, pl=8,pu=40,drift=TRUE)
unemp.tr3 <- trfilter(unemp, pl=2,pu=60,drift=TRUE)
unemp.tr4 <- trfilter(unemp, pl=2,pu=40,drift=TRUE)

par(mfrow=c(2,1),mar=c(3,3,2,1),cex=.8)
plot(unemp.tr1$x,
     main="Trigonometric regression filter of unemployment: Trend, drift=TRUE",
     col=1, ylab="")
lines(unemp.tr1$trend,col=2)
lines(unemp.tr2$trend,col=3)
lines(unemp.tr3$trend,col=4)
lines(unemp.tr4$trend,col=5)
legend("topleft",legend=c("series", "pl=2, pu=32", "pl=8, pu=40",
"pl=2, pu=60", "pl=2, pu=40"), col=1:5, lty=rep(1,5), ncol=1)

plot(unemp.tr1$cycle,
     main="Trigonometric regression filter of unemployment: Cycle,drift=TRUE",
     col=2, ylab="", ylim=range(unemp.tr3$cycle,na.rm=TRUE))
lines(unemp.tr2$cycle,col=3)
lines(unemp.tr3$cycle,col=4)
lines(unemp.tr4$cycle,col=5)
```

```
## legend("topleft", legend=c("p1=2, pu=32", "p1=8, pu=40", "p1=2, pu=60",
## "p1=2, pu=40"), col=1:5, lty=rep(1,5), ncol=1)

par(opar)
```

---

unemp

*US Quarterly Unemployment Series*


---

### Description

Quarterly US unemployment series for 1959.1 to 2000.4.

*number of observations* : 168

*observation* : country

*country* : United States

### Usage

```
data(unemp)
```

### Format

A time series containing :

**unemp** unemployment rate (average of months in quarter)

### Author(s)

Mehmet Balcilar, (mbalcilar@yahoo.com)

### Source

Bureau of Labor Statistics, OECD, Federal Reserve.

### References

Stock, James H. and Mark W. Watson (2003) *Introduction to Econometrics*, Addison-Wesley Educational Publishers, [http://wps.aw.com/aw\\_stockwatsn\\_economtrcs\\_1](http://wps.aw.com/aw_stockwatsn_economtrcs_1), chapter 12 and 14.

### Examples

```
## library(mFilter)

data(unemp)

unemp.hp <- mFilter(unemp, filter="HP") # Hodrick-Prescott filter
unemp.bk <- mFilter(unemp, filter="BK") # Baxter-King filter
unemp.cf <- mFilter(unemp, filter="CF") # Christiano-Fitzgerald filter
```



```
opar <- par(no.readonly=TRUE)
par(mfrow=c(2,1),mar=c(3,3,2,1))
plot(unemp,main="Unemployment Series & Estimated Trend",col=1,ylab="")
lines(unemp.hp$trend,col=2)
lines(unemp.bk$trend,col=3)
lines(unemp.cf$trend,col=4)
legend("topleft",legend=c("series", "HP", "BK", "CF"),col=1:4,
      lty=rep(1,4),ncol=2)

plot(unemp.hp$cycle,main="Estimated Cyclical Component",col=2,
      ylim=c(-2,2),ylab="")
lines(unemp.bk$cycle,col=3)
lines(unemp.cf$cycle,col=4)
legend("topleft",legend=c("HP", "BK", "CF"),col=2:4,lty=rep(1,3),ncol=2)
par(opar)
```

# Index

## \*Topic **datasets**

unemp, [23](#)

## \*Topic **loess**

bkfilter, [1](#)

bwfilter, [4](#)

cffilter, [7](#)

hpfilter, [10](#)

mFilter, [17](#)

mFilter-methods, [13](#)

mFilter-package, [14](#)

trfilter, [20](#)

## \*Topic **nonparametric**

bkfilter, [1](#)

bwfilter, [4](#)

cffilter, [7](#)

hpfilter, [10](#)

mFilter, [17](#)

mFilter-methods, [13](#)

mFilter-package, [14](#)

trfilter, [20](#)

## \*Topic **smooth**

bkfilter, [1](#)

bwfilter, [4](#)

cffilter, [7](#)

hpfilter, [10](#)

mFilter, [17](#)

mFilter-methods, [13](#)

mFilter-package, [14](#)

trfilter, [20](#)

## \*Topic **ts**

bkfilter, [1](#)

bwfilter, [4](#)

cffilter, [7](#)

hpfilter, [10](#)

mFilter, [17](#)

mFilter-methods, [13](#)

mFilter-package, [14](#)

trfilter, [20](#)

bkfilter, [1](#), [6](#), [9](#), [12](#), [14](#), [17](#), [19](#), [22](#)

bwfilter, [3](#), [4](#), [9](#), [12](#), [14](#), [17](#), [19](#), [22](#)

cffilter, [3](#), [6](#), [7](#), [12](#), [14](#), [17](#), [19](#), [22](#)

fitted.mFilter, [19](#)

fitted.mFilter (*mFilter-methods*),  
[13](#)

hpfilter, [3](#), [6](#), [9](#), [10](#), [17](#), [22](#)

interactive, [13](#)

mFilter, [3](#), [5](#), [6](#), [9](#), [11–14](#), [17](#), [17](#), [22](#)

mFilter-methods, [17](#)

mFilter-methods, [13](#)

mFilter-package, [14](#)

numeric, [18](#)

plot, [13](#)

plot.mFilter, [19](#)

plot.mFilter (*mFilter-methods*), [13](#)

print, [13](#)

print.mFilter, [19](#)

print.mFilter (*mFilter-methods*),  
[13](#)

residuals.mFilter, [19](#)

residuals.mFilter  
(*mFilter-methods*), [13](#)

summary.mFilter, [19](#)

summary.mFilter  
(*mFilter-methods*), [13](#)

trfilter, [3](#), [6](#), [9](#), [12](#), [14](#), [17](#), [19](#), [20](#)

ts, [18](#)

unemp, [23](#)

vector, [18](#)